$E_{N}=E_{A}+E_{R} \quad E_{\text {total }}=-\frac{A}{r}+\frac{B}{r^{n}} \quad A=\frac{z_{1} z_{2} e^{2}}{4 \pi \varepsilon_{o}} \quad E=\int F d r \quad F=\frac{d E}{d r}$
Density $=\frac{\text { mass }}{\text { volume }} ; \quad \rho=\frac{n A}{V_{c} N_{A}} ; \quad A P F=\frac{V_{\text {atoms }}}{V_{\text {unit cell }}} ;$
Volume of a sphere $=\frac{4}{3} \pi r^{3} \quad$ \% ionic character $=\left(1-e^{-\frac{\left(X_{A}-X_{B}\right)^{2}}{4}}\right) \times 100 \%$

$$
\begin{array}{llrl}
N_{v}=N \exp \left(-\frac{Q_{v}}{k T}\right) ; & N=\frac{N_{A} \rho}{A} ; & J=-D \frac{d C}{d x} \quad \frac{\Delta C}{\Delta x}=\frac{C_{2}-C_{1}}{x_{2}-x_{1}} \\
D=D_{o} \exp \left(-\frac{Q_{d}}{R T}\right) ; & \frac{\partial C}{\partial t}=D \frac{\partial^{2} C}{\partial x^{2}} ; & \frac{C(x, t)-C_{o}}{C_{s}-C_{o}}=1-\operatorname{erf}\left(\frac{x}{2 \sqrt{D t}}\right) & x \approx \sqrt{D t}
\end{array}
$$

$$
\sigma=\frac{F}{A_{0}} \quad \sigma=\mathrm{E} \varepsilon \quad \varepsilon=\frac{\delta}{L_{0}} \quad v=-\frac{\varepsilon_{l}}{\varepsilon} \quad \varepsilon L=\frac{-\delta L}{W_{0}} \quad U_{r} \cong \frac{1}{2} \sigma_{y} \varepsilon_{y} \quad \tau=G \gamma
$$

$\% E L=\frac{L_{f}-L_{0}}{L_{0}} \times 100 \quad \% R A=\frac{A_{o}-A_{f}}{A_{0}} \times 100 \quad W_{L}=\frac{M_{L}}{M_{L}+M_{\alpha}}=\frac{S}{R+S}=\frac{C_{a}-C_{0}}{C_{a}-C_{L}} \quad W_{a}=\frac{R}{R+S}=\frac{C_{0}-C_{L}}{C_{a}-C_{L}}$

$$
D P_{n}=\sum x_{i} n_{i}=\frac{\overline{M_{n}}}{m} \quad D P_{w}=\sum w_{i} n_{i}=\frac{\overline{M_{w}}}{m} \quad m=\Sigma f_{i} m_{i} \quad \rho=\frac{n^{\prime}\left(\Sigma A_{\mathrm{C}}+\Sigma A_{\mathrm{A}}\right)}{V_{C} N_{\mathrm{A}}}
$$

$\rho=\frac{(\# \text { of cations/UC)(atomic wt. of cation) }+ \text { (\# of anions/UC)(atomic wt. of anion) }}{V_{C} N_{A}}$

$$
\begin{gathered}
\Delta \mathrm{V}=\mathrm{V}_{2}^{\circ}-\mathrm{V}_{1}^{\circ}-\frac{\mathrm{RT}}{\mathrm{nF}} \ln \frac{\left[\mathrm{M}_{1}^{\mathrm{n}+}\right]}{\left[\mathrm{M}_{2}^{\mathrm{n}+}\right]} \quad \Delta \mathrm{V}=\mathrm{V}_{2}^{\circ}-\mathrm{V}_{1}^{\circ}-\frac{0.0592}{\mathrm{n}} \log \frac{\left[\mathrm{M}_{1}^{\mathrm{n}+}\right]}{\left[\mathrm{M}_{2}^{\mathrm{n}+}\right]} \\
\mathrm{CPR}=\frac{\mathrm{KW}}{\rho \mathrm{At}} \quad J=\sigma \mathrm{E} \quad J=e v_{d} n \quad \mathrm{~V}_{\mathrm{d}}=\mu_{e^{\mathrm{E}}} \quad \sigma_{\mathrm{undoped}} \propto e^{-\frac{-E_{g a p}}{k T}} \\
\sigma=\mathrm{n}|e| \mu_{e}+p|e| \mu_{h}
\end{gathered}
$$

## Useful constants:

Avogadro's \#: $6.023 \times 10^{23}$ atoms $/ \mathrm{mol}$. Electronic charge: $\mathrm{e}=-1.602 \times 10^{-19} \mathrm{C}$
Boltzmann's constant: $\mathrm{k}=1.38 \times 10^{-23} \mathrm{~J} /$ atom $-\mathrm{K}=8.62 \times 10^{-5} \mathrm{eV} /$ atom -K
Planck's constant: $\mathrm{h}=6.625 \times 10^{-34} \mathrm{~J}-\mathrm{s} \quad$ Bohr Magneton: $\mathrm{m}_{\mathrm{B}}=9.27 \times 10^{-24} \mathrm{~A}-\mathrm{m}^{2}$
Gas Constant: $\mathrm{R}=8.31 \mathrm{~J} / \mathrm{mol}-\mathrm{K}=1.987 \mathrm{cal} / \mathrm{mol}-\mathrm{K}$
Gravitational constant: $\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}$
Faraday Constant: F = 96,487 C/mol

Table 17.2 The Galvanic Series

|  | Platinum |
| :---: | :---: |
|  | Gold |
|  | Graphite |
|  | Titanium |
|  | Silver |
|  | [316 Stainless steel (passive) |
|  | 304 Stainless steel (passive) |
| Increasingly inert (cathodic) | $\left[\begin{array}{l}\text { Inconel ( } 80 \mathrm{Ni}-13 \mathrm{Cr}-7 \mathrm{Fe} \text { ) (passive) } \\ \text { Nickel (passive) }\end{array}\right.$ |
|  | [Monel (70Ni-30Cu) |
|  | Copper-nickel alloys |
|  | Bronzes ( $\mathrm{Cu}-\mathrm{Sn}$ alloys) |
|  | Copper |
|  | Brasses ( $\mathrm{Cu}-\mathrm{Zn}$ alloys) |
|  | [ Inconel (active) |
|  | L Nickel (active) |
|  | Tin |
|  | Lead |
| Increasingly active (anodic) | 316 Stainless steel (active) |
|  | 304 Stainless steel (active) |
|  | [ Cast iron |
|  | Iron and steel |
|  | Aluminum alloys |
|  | Cadmium |
|  | Commercially pure aluminum |
|  | Zinc |
|  | Magnesium and magnesium alloys |

Table 17.1 The Standard emf Series

| Electrode Reaction | Standard Electrode <br> Potential, $\boldsymbol{V}^{\mathbf{0}} \mathbf{( V )}$ |  |
| :---: | :---: | :---: |
| $\uparrow$ | $\mathrm{Au}^{3+}+3 e^{-} \longrightarrow \mathrm{Au}$ | +1.420 |
|  | $\mathrm{O}_{2}+4 \mathrm{H}^{+}+4 e^{-} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}$ | +1.229 |
| $\mathrm{Pt}^{2+}+2 e^{-} \longrightarrow \mathrm{Pt}$ | $\sim+1.2$ |  |
| Increasingly inert | $\mathrm{Ag}^{-}+e^{-} \longrightarrow \mathrm{Ag}$ | +0.800 |
| (cathodic) | $\mathrm{Fe}^{3+}+e^{-} \longrightarrow \mathrm{Fe}^{2+}$ | +0.771 |
|  | $\mathrm{O}_{2}+2 \mathrm{H}_{2} \mathrm{O}+4 e^{-} \longrightarrow 4\left(\mathrm{OH}^{-}\right)$ | +0.401 |
| $\mathrm{Cu}^{2+}+2 e^{-} \longrightarrow \mathrm{Cu}$ | +0.340 |  |
|  | $2 \mathrm{H}^{+}+2 e^{-} \longrightarrow \mathrm{H}$ | 0.000 |
|  | $\mathrm{~Pb}^{2+}+2 e^{-} \longrightarrow \mathrm{Pb}$ | -0.126 |
| $\mathrm{Sn}^{2+}+2 e^{-} \longrightarrow \mathrm{Pn}$ | -0.136 |  |
| Increasingly active | $\mathrm{Ni}^{2+}+2 e^{-} \longrightarrow \mathrm{Ni}$ | -0.250 |
| $($ anodic) | $\mathrm{Co}^{2+}+2 e^{-} \longrightarrow \mathrm{Co}$ | -0.277 |
|  | $\mathrm{Cd}^{2+}+2 e^{-} \longrightarrow \mathrm{Cd}$ | -0.403 |
|  | $\mathrm{Fe}^{2+}+2 e^{-} \longrightarrow \mathrm{Fe}$ | -0.440 |
|  | $\mathrm{Cr}^{3+}+3 e^{-} \longrightarrow \mathrm{Cr}$ | -0.744 |
|  | $\mathrm{Zn}^{2+}+2 e^{-} \longrightarrow \mathrm{Zn}$ | -0.763 |
|  | $\mathrm{Al}^{3+}+3 e^{-} \longrightarrow \mathrm{Al}$ | -1.662 |
|  | $\mathrm{Mg}^{2+}+2 e^{-} \longrightarrow \mathrm{Mg}$ | -2.363 |
|  | $\mathrm{Na}^{+}+e^{-} \longrightarrow \mathrm{Na}$ | -2.714 |
|  | $\mathrm{~K}^{+}+e^{-} \longrightarrow \mathrm{K}$ | -2.924 |

Table 12.3 Ionic Radii for Several Cations and Anions (for a Coordination Number of 6)

| Cation | Ionic Radius <br> $(\boldsymbol{n m})$ | Anion | Ionic Radius <br> $(\boldsymbol{n m})$ |
| :--- | :---: | :---: | :---: |
| $\mathrm{Al}^{3+}$ | 0.053 | $\mathrm{Br}^{-}$ | 0.196 |
| $\mathrm{Ba}^{2+}$ | 0.136 | $\mathrm{Cl}^{-}$ | 0.181 |
| $\mathrm{Ca}^{2+}$ | 0.100 | $\mathrm{~F}^{-}$ | 0.133 |
| $\mathrm{Cs}^{+}$ | 0.170 | $\mathrm{I}^{-}$ | 0.220 |
| $\mathrm{Fe}^{2+}$ | 0.077 | $\mathrm{O}^{2-}$ | 0.140 |
| $\mathrm{Fe}^{3+}$ | 0.069 | $\mathrm{~S}^{2-}$ | 0.184 |
| $\mathrm{~K}^{+}$ | 0.138 |  |  |
| $\mathrm{Mg}^{2+}$ | 0.072 |  |  |
| $\mathrm{Mn}^{2+}$ | 0.067 |  |  |
| $\mathrm{Na}^{+}$ | 0.102 |  |  |
| $\mathrm{Ni}^{2+}$ | 0.069 |  |  |
| $\mathrm{Si}^{4+}$ | 0.040 |  |  |
| $\mathrm{Ti}^{4+}$ | 0.061 |  |  |

Table 5.1 Tabulation of Error Function Values

| $z$ | $\operatorname{erf}(z)$ | $z$ | $\operatorname{erf}(z)$ | $z$ | $\operatorname{erf}(z)$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| 0 | 0 | 0.55 | 0.5633 | 1.3 | 0.9340 |
| 0.025 | 0.0282 | 0.60 | 0.6039 | 1.4 | 0.9523 |
| 0.05 | 0.0564 | 0.65 | 0.6420 | 1.5 | 0.9661 |
| 0.10 | 0.1125 | 0.70 | 0.6778 | 1.6 | 0.9763 |
| 0.15 | 0.1680 | 0.75 | 0.7112 | 1.7 | 0.9838 |
| 0.20 | 0.2227 | 0.80 | 0.7421 | 1.8 | 0.9891 |
| 0.25 | 0.2763 | 0.85 | 0.7707 | 1.9 | 0.9928 |
| 0.30 | 0.3286 | 0.90 | 0.7970 | 2.0 | 0.9953 |
| 0.35 | 0.3794 | 0.95 | 0.8209 | 2.2 | 0.9981 |
| 0.40 | 0.4284 | 1.0 | 0.8427 | 2.4 | 0.9993 |
| 0.45 | 0.4755 | 1.1 | 0.8802 | 2.6 | 0.9998 |
| 0.50 | 0.5205 | 1.2 | 0.9103 | 2.8 | 0.9999 |



